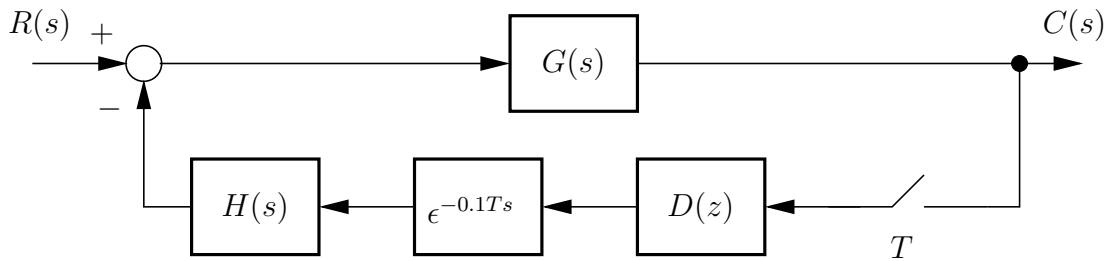


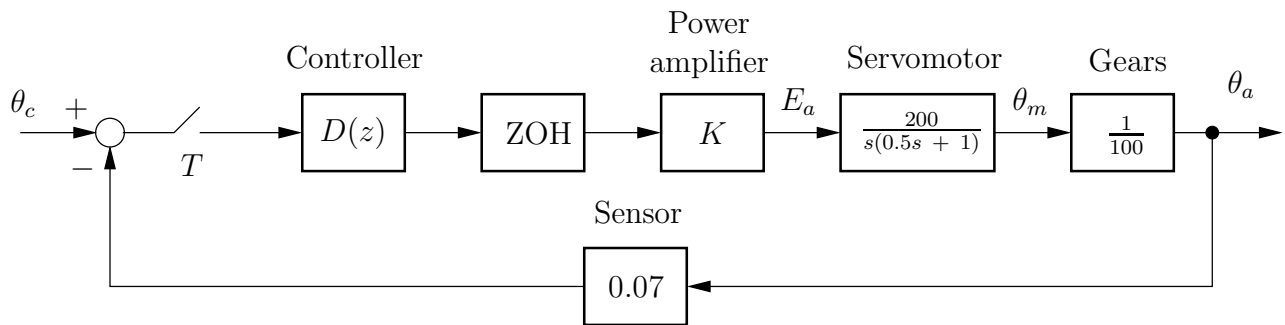
EE 233 Homework 6.

5-11. In the system below, the ideal time delay represents the time required to complete the computations in the computer.



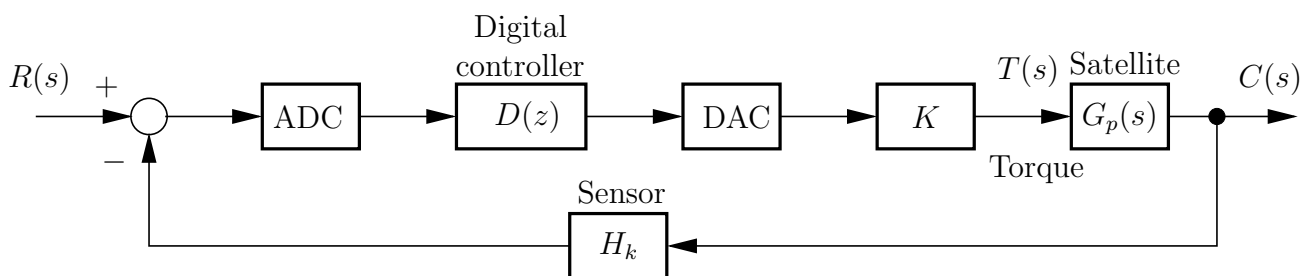
- Derive the output function  $C(z)$  for this system.
- Suppose that the ideal delay is associated with the sensor rather than the computer, and the position of  $H(s)$  and the ideal delay are reversed. Find  $C(z)$  for this case.

5-13. Consider the robot-joint control system below.



- Find the system transfer function in terms of  $T$ ,  $D(z)$  and  $K$ .
- Evaluate the system transfer function for  $T = 0.1 \text{ s}$ ,  $K = 2.4$  and  $D(z) = 1$ .

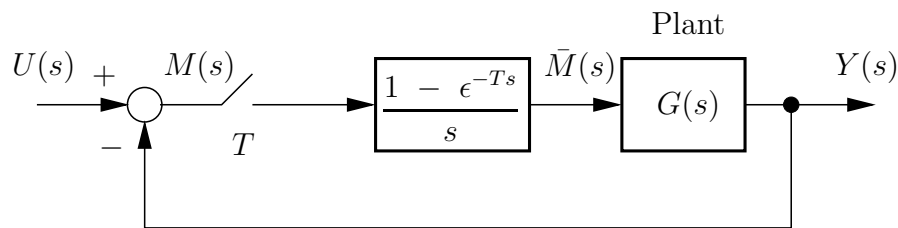
5-14. Consider the satellite control system below. Let  $H_k = 0.02$ .



- Find the system transfer function in terms of  $D(z)$ ,  $K$  and  $H_k$ .

b. Evaluate the system transfer function for  $D(z) = 1$ ,  $K = 2$  and  $T = 1$ .

5-20. Suppose that the plant in the following figure



has the discrete state model

$$\begin{aligned}x(k + 1) &= Ax(k) + Bm(k) \\y(k) &= Cx(k) + Dm(k)\end{aligned}$$

Derive the state model for the closed-loop system in terms of  $A$ ,  $B$ ,  $C$  and  $D$ .

5-21. Find a discrete state variable model of the closed-loop system in Problem 5-20 if the discrete state model of the plant is given by

a.

$$\begin{aligned}x(k + 1) &= 0.7x(k) + 0.3m(k) \\y(k) &= 0.2x(k) + 0.5u(k)\end{aligned}$$

b.

$$\begin{aligned}x(k + 1) &= \begin{bmatrix} 0 & 1 \\ -0.9 & 1.3 \end{bmatrix} x(k) + \begin{bmatrix} 0.1 \\ 0.05 \end{bmatrix} m(k) \\y(k) &= \begin{bmatrix} 1.2 & -0.7 \end{bmatrix} x(k)\end{aligned}$$

c.

$$\begin{aligned}x(k + 1) &= \begin{bmatrix} 0.5 & 0 & 0 \\ 0 & 0.9 & 1 \\ -1 & 0 & 0.9 \end{bmatrix} x(k) + \begin{bmatrix} 1 \\ 0 \\ 2 \end{bmatrix} m(k) \\y(k) &= \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} x(k)\end{aligned}$$